

SCHAUM'S OUTLINE OF
THEORY AND PROBLEMS

OF

**FEEDBACK and
CONTROL SYSTEMS**

Second Edition

CONTINUOUS (ANALOG) AND DISCRETE (DIGITAL)

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SCHAUM'S OUTLINE SERIES

McGRAW-HILL

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