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## MATHEMATICS

## Course Structure

| Units | Topics | Marks |
| :--- | :--- | :---: |
| I | Relations and Functions | 10 |
| II | Algebra | 13 |
| III | Calculus | 44 |
| IV | Vectors and 3-D Geometry | 17 |
| V | Linear Programming | 6 |
| VI | Probability | 10 |
| Total |  | $\mathbf{1 0 0}$ |

## Course Syllabus

## Unit I: Relations and Functions

## Chapter 1: Relations and Functions

> Types of relations:

- Reflexive
- Symmetric
- transitive and equivalence relations
- One to one and onto functions
- composite functions
- inverse of a function
- Binary operations


## Chapter 2: Inverse Trigonometric Functions

> Definition, range, domain, principal value branch
$>$ Graphs of inverse trigonometric functions
> Elementary properties of inverse trigonometric functions

## Unit II: Algebra

## Chapter 1: Matrices

> Concept, notation, order, equality, types of matrices, zero and identity matrix, transpose of a matrix, symmetric and skew symmetric matrices.
> Operation on matrices: Addition and multiplication and multiplication with a scalar
> Simple properties of addition, multiplication and scalar multiplication
> Noncommutativity of multiplication of matrices and existence of non-zero matrices whose product is the zero matrix (restrict to square matrices of order 2)
> Concept of elementary row and column operations
> Invertible matrices and proof of the uniqueness of inverse, if it exists; (Here all matrices will have real entries).

## Chapter 2: Determinants

> Determinant of a square matrix (up to $3 \times 3$ matrices), properties of determinants, minors, co-factors and applications of determinants in finding the area of a triangle
> Ad joint and inverse of a square matrix
$>$ Consistency, inconsistency and number of solutions of system of linear equations by examples, solving system of linear equations in two or three variables (having unique solution) using inverse of a matrix

## Unit III: Calculus

## Chapter 1: Continuity and Differentiability

> Continuity and differentiability, derivative of composite functions, chain rule, derivatives of inverse trigonometric functions, derivative of implicit functions
> Concept of exponential and logarithmic functions.
> Derivatives of logarithmic and exponential functions
> Logarithmic differentiation, derivative of functions expressed in parametric forms. Second order derivatives
> Rolle's and Lagrange's Mean Value Theorems (without proof) and their geometric interpretation

## Chapter 2: Applications of Derivatives

> Applications of derivatives: rate of change of bodies, increasing/decreasing functions, tangents and normal, use of derivatives in approximation, maxima and minima (first derivative test motivated geometrically and second derivative test given as a provable tool)
> Simple problems (that illustrate basic principles and understanding of the subject as well as real-life situations)

## Chapter 3: Integrals

> Integration as inverse process of differentiation
> Integration of a variety of functions by substitution, by partial fractions and by parts
$>$ Evaluation of simple integrals of the following types and problems based on them
$\int \frac{d x}{x^{2} \pm a^{2}}, \int \frac{d x}{\sqrt{x^{2} \pm a^{2}}}, \int \frac{d x}{\sqrt{a^{2}-x^{2}}}, \int \frac{d x}{a x^{2}+b x+c} \int \frac{d x}{\sqrt{a x^{2}+b x+c}}$
$\int \frac{p x+q}{a x^{2}+b x+c} d x, \int \frac{p x+q}{\sqrt{a x^{2}+b x+c}} d x, \int \sqrt{a^{2} \pm x^{2}} d x, \int \sqrt{x^{2}-a^{2}} d x$

$$
\int \sqrt{a x^{2}+b x+c} d x, \int(p x+q) \sqrt{a x^{2}+b x+c} d x
$$

> Definite integrals as a limit of a sum, Fundamental Theorem of Calculus (without proof)
> Basic properties of definite integrals and evaluation of definite integrals

## Chapter 4: Applications of the Integrals

> Applications in finding the area under simple curves, especially lines, circles/parabolas/ellipses (in standard form only)
> Area between any of the two above said curves (the region should be clearly identifiable)

## Chapter 5: Differential Equations

> Definition, order and degree, general and particular solutions of a differential equation
> Formation of differential equation whose general solution is given
> Solution of differential equations by method of separation of variables solutions of homogeneous differential equations of first order and first degree
$>$ Solutions of linear differential equation of the type:

- $d y / d x+p y=q$, where $p$ and $q$ are functions of $x$ or constants
- $d x / d y+p x=q$, where $p$ and $q$ are functions of $y$ or constants


## Unit IV: Vectors and Three-Dimensional Geometry

## Chapter 1: Vectors

> Vectors and scalars, magnitude and direction of a vector
> Direction cosines and direction ratios of a vector
> Types of vectors (equal, unit, zero, parallel and collinear vectors), position vector of a point, negative of a vector, components of a vector, addition of vectors, multiplication of a vector by a scalar, position vector of a point dividing a line segment in a given ratio
> Definition, Geometrical Interpretation, properties and application of scalar (dot) product of vectors, vector (cross) product of vectors, scalar triple product of vectors

## Chapter 2: Three - dimensional Geometry

> Direction cosines and direction ratios of a line joining two points
> Cartesian equation and vector equation of a line, coplanar and skew lines, shortest distance between two lines
> Cartesian and vector equation of a plane
> Angle between:

- Two lines
- Two planes
- A line and a plane
> Distance of a point from a plane


## Unit V: Linear Programming

## Chapter 1: Linear Programming

> Introduction
> Related terminology such as:

- Constraints
- Objective function
- Optimization
- Different types of linear programming (L.P.) Problems
- Mathematical formulation of L.P. Problems
- Graphical method of solution for problems in two variables
- Feasible and infeasible regions (bounded and unbounded)
- Feasible and infeasible solutions
- Optimal feasible solutions (up to three non-trivial constraints)


## Unit VI: Probability

## Chapter 1: Probability

> Conditional probability
> Multiplication theorem on probability
> Independent events, total probability
> Baye's theorem
> Random variable and its probability distribution
> Mean and variance of random variable
> Repeated independent (Bernoulli) trials and Binomial distribution

