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# **MATHEMATICS**

#### **Course Structure**

Units	Topics	Marks
Ι	Relations and Functions	10
II	Algebra	13
III	Calculus	44
IV	Vectors and 3-D Geometry	17
V	Linear Programming	6
VI	Probability	10
Total	•	100

# **Course Syllabus**

# **Unit I: Relations and Functions**

# **Chapter 1: Relations and Functions**

- > Types of relations:
  - Reflexive
  - Symmetric
  - transitive and equivalence relations
  - One to one and onto functions
  - composite functions
  - inverse of a function
  - Binary operations

# **Chapter 2: Inverse Trigonometric Functions**

- > Definition, range, domain, principal value branch
- > Graphs of inverse trigonometric functions



Elementary properties of inverse trigonometric functions

# Unit II: Algebra

### **Chapter 1: Matrices**

- Concept, notation, order, equality, types of matrices, zero and identity matrix, transpose of a matrix, symmetric and skew symmetric matrices.
- Operation on matrices: Addition and multiplication and multiplication with a scalar
- > Simple properties of addition, multiplication and scalar multiplication
- Noncommutativity of multiplication of matrices and existence of non-zero matrices whose product is the zero matrix (restrict to square matrices of order
   2)
- Concept of elementary row and column operations
- Invertible matrices and proof of the uniqueness of inverse, if it exists; (Here all matrices will have real entries).

#### **Chapter 2: Determinants**

- ➤ Determinant of a square matrix (up to 3 x 3 matrices), properties of determinants, minors, co-factors and applications of determinants in finding the area of a triangle
- Ad joint and inverse of a square matrix
- Consistency, inconsistency and number of solutions of system of linear equations by examples, solving system of linear equations in two or three variables (having unique solution) using inverse of a matrix



#### **Unit III: Calculus**

### **Chapter 1: Continuity and Differentiability**

- Continuity and differentiability, derivative of composite functions, chain rule, derivatives of inverse trigonometric functions, derivative of implicit functions
- Concept of exponential and logarithmic functions.
- Derivatives of logarithmic and exponential functions
- Logarithmic differentiation, derivative of functions expressed in parametric forms. Second order derivatives
- Rolle's and Lagrange's Mean Value Theorems (without proof) and their geometric interpretation

#### **Chapter 2: Applications of Derivatives**

- Applications of derivatives: rate of change of bodies, increasing/decreasing functions, tangents and normal, use of derivatives in approximation, maxima and minima (first derivative test motivated geometrically and second derivative test given as a provable tool)
- Simple problems (that illustrate basic principles and understanding of the subject as well as real-life situations)

#### **Chapter 3: Integrals**

- Integration as inverse process of differentiation
- Integration of a variety of functions by substitution, by partial fractions and by parts
- > Evaluation of simple integrals of the following types and problems based on them

$$\int \frac{dx}{x^2 \pm a^2}, \int \frac{dx}{\sqrt{x^2 \pm a^2}}, \int \frac{dx}{\sqrt{a^2 - x^2}}, \int \frac{dx}{ax^2 + bx + c} \int \frac{dx}{\sqrt{ax^2 + bx + c}}$$

$$\int \frac{px + q}{ax^2 + bx + c} dx, \int \frac{px + q}{\sqrt{ax^2 + bx + c}} dx, \int \sqrt{a^2 \pm x^2} dx, \int \sqrt{x^2 - a^2} dx$$



$$\int \sqrt{ax^2 + bx + c} \, dx, \int (px + q) \sqrt{ax^2 + bx + c} \, dx$$

- Definite integrals as a limit of a sum, Fundamental Theorem of Calculus (without proof)
- > Basic properties of definite integrals and evaluation of definite integrals

# **Chapter 4: Applications of the Integrals**

- Applications in finding the area under simple curves, especially lines, circles/parabolas/ellipses (in standard form only)
- > Area between any of the two above said curves (the region should be clearly identifiable)

### **Chapter 5: Differential Equations**

- Definition, order and degree, general and particular solutions of a differential equation
- > Formation of differential equation whose general solution is given
- > Solution of differential equations by method of separation of variables solutions of homogeneous differential equations of first order and first degree
- > Solutions of linear differential equation of the type:
  - dy/dx + py = q, where p and q are functions of x or constants
  - dx/dy + px = q, where p and q are functions of y or constants

# **Unit IV: Vectors and Three-Dimensional Geometry**

#### **Chapter 1: Vectors**

Vectors and scalars, magnitude and direction of a vector



- > Direction cosines and direction ratios of a vector
- > Types of vectors (equal, unit, zero, parallel and collinear vectors), position vector of a point, negative of a vector, components of a vector, addition of vectors, multiplication of a vector by a scalar, position vector of a point dividing a line segment in a given ratio
- Definition, Geometrical Interpretation, properties and application of scalar (dot) product of vectors, vector (cross) product of vectors, scalar triple product of vectors

# **Chapter 2: Three - dimensional Geometry**

- > Direction cosines and direction ratios of a line joining two points
- Cartesian equation and vector equation of a line, coplanar and skew lines, shortest distance between two lines
- Cartesian and vector equation of a plane
- Angle between:
  - Two lines
  - Two planes
  - A line and a plane
- > Distance of a point from a plane

# **Unit V: Linear Programming**

#### **Chapter 1: Linear Programming**

- > Introduction
- Related terminology such as:
  - Constraints
  - Objective function
  - Optimization
  - Different types of linear programming (L.P.) Problems
  - Mathematical formulation of L.P. Problems
  - Graphical method of solution for problems in two variables



- Feasible and infeasible regions (bounded and unbounded)
- Feasible and infeasible solutions
- Optimal feasible solutions (up to three non-trivial constraints)

# **Unit VI: Probability**

# **Chapter 1: Probability**

- > Conditional probability
- > Multiplication theorem on probability
- > Independent events, total probability
- > Baye's theorem
- > Random variable and its probability distribution
- > Mean and variance of random variable
- > Repeated independent (Bernoulli) trials and Binomial distribution

