Algebra 1 Unit 3C – Test Review – answer key

Part One: Graphing Quadratics

Graph the following quadratic functions.



vertex @ (6,4) – goes in middle of table

| x | f(x) | |
|---|------|---|
| 4 | 6 | 6- 5- 4- |
| 5 | 4.5 | 3- 2- 1- x |
| 6 | 4 | _9 _8 _7 _6 _5 _4 _3 _2 _1_1 _ 1 _2 _3 _4 _5 _6 _7 _8 9 ' _2- _3- |
| 7 | 4.5 | 4+ |
| 8 | 6 | |

5) $f(x) = (x + 2)^2 - 1$ a = 1 h = -2 k = -1vertex @ (-2, -1) - goes in middle of table





4)
$$f(x) = x^2 - 3$$

$$a = 1 \qquad h = 0 \qquad k = -3$$





6)
$$f(x) = -4x^2 + 8$$

 $a = -4$ $h = 0$ $k = 8$





Part Two: Characteristics of Graphs

Identify the listed characteristics for each graph.



Range: $[-3, \infty)$ Vertex: (-1, -3)Extrema/extrema value: minimum at y = -3

Domain: $(-\infty, \infty)$ or all real numbers

Axis of Symmetry: x = -1



Y-Intercept: (0,9)

X-Intercept(s): (-3,0) and (6,0)

Solution(s): x = -3 and x = 6

Extrema type: maximum



Domain: $(-\infty, \infty)$ or all real numbers Range: $[-7, \infty)$ Vertex: (1, -7)Axis of Symmetry: x = 1Y-Intercept: (0, -5)X-Intercept(s): (-1, 0) and (3, 0)Extrema/extrema value: minimum at y = -7Solution(s): x = -1 and x = 3

Part Three: Average Rate of Change

Find the average rate of change indicated for each function below.

10) Find the average rate of change over the interval [0, 2].







Part Four: Transformations of Quadratic Functions

Identify the transformations for each function below from the parent function $f(x) = x^2$.

12) $f(x) = -x^2 + 5$ 13) $f(x) = 2(x+4)^2$ $a = -1 \rightarrow$ reflection over x-axis $a = 2 \rightarrow$ vertical stretch of 2 $h = -4 \rightarrow$ translation left 4 units h = 0 $k = 5 \rightarrow$ translation up 5 units k = 014) $f(x) = -3(x-6)^2 - 2$ 15) $f(x) = (x+1)^2$ $a = -3 \rightarrow$ reflection over x-axis a = 1and vertical stretch of 3 $h = 6 \rightarrow$ translation right 6 units $h = -1 \rightarrow$ translation left 1 units $k = -2 \rightarrow$ translation down 2 units k = 016) $f(x) = 4(x+3)^2 + 1$ 17) $f(x) = -\frac{1}{2}(x-4)^2 - 3$ $a = -\frac{1}{2} \rightarrow$ reflection over x-axis $a = 4 \rightarrow$ vertical stretch of 4 vertical shrink of $\frac{1}{2}$ $h = -3 \rightarrow$ translation left 3 units $h = 4 \rightarrow$ translation right 4 units $k = -3 \rightarrow$ translation down 3 units $k = 1 \rightarrow$ translation up 1 units

Part Five: Vertex, Axis of Symmetry, and Extrema

For the following functions, identify the vertex, axis of symmetry and extrema.

18) $f(x) = x^2 - 6x + 1$ 19) $f(x) = -2x^2 + 12x$ vertex: $x = \frac{-b}{2a} = \frac{6}{2(1)} = \frac{6}{2} = 3$ vertex: $x = \frac{-b}{2a} = \frac{-12}{2(-2)} = \frac{-12}{-4} = 3$ $y = (3)^2 - 6(3) + 1 = -8$ $y = -2(3)^2 + 12(3) = 18$ vertex: (3, -8)vertex: (3, 18)axis of symmetry: x = 3axis of symmetry: x = 3extrema: minimum (since a is +)extrema: maximum (since a is -)

20) $f(x) = 3(x+4)^2 - 1$ a = 3 h = -4 k = -1

vertex: (-4, -1)axis of symmetry: x = -4extrema: minimum (since a is +) 21) $f(x) = -2(x-3)^2 + 5$

 $a = -2 \quad h = 3 \quad k = 5$

vertex: (3, 5)axis of symmetry: x = 3extrema: maximum (since a is -)

Part Six: Converting Between Different Forms of Quadratics

Convert the following quadratic functions from vertex form to standard form.

| 22) $f(x) = -0.5(x+4)^2 - 2$ | 23) $f(x) = 3(x-1)^2 + 4$ |
|---------------------------------------|-----------------------------------|
| f(x) = -0.5(x+4)(x+4) - 2 | f(x) = 3(x-1)(x-1) + 4 |
| $f(x) = -0.5(x^2 + 4x + 4x + 16) - 2$ | $f(x) = 3(x^2 - 1x - 1x + 1) + 4$ |
| $f(x) = -0.5(x^2 + 8x + 16) - 2$ | $f(x) = 3(x^2 - 2x + 1) + 4$ |
| $f(x) = -0.5x^2 - 4x - 8 - 2$ | $f(x) = 3x^2 - 6x + 3 + 4$ |
| $f(x) = -0.5x^2 - 4x - 10$ | $f(x) = 3x^2 - 6x + 7$ |

Convert the following quadratic functions from standard form to vertex form.

| 24) $f(x) = 2x^2 + 8x - 6$ | 25) $f(x) = -x^2 + 6x + 3$ |
|---|--|
| a = 2 b = 8 c = -6 | a = -1 b = 6 c = 3 |
| vertex: $x = \frac{-b}{2a} = \frac{-8}{2(2)} = \frac{-8}{4} = -2 \rightarrow h$ | vertex: $x = \frac{-b}{2a} = \frac{-6}{2(-1)} = \frac{-6}{-2} = 3 \rightarrow h$ |
| $y = 2(-2)^2 + 8(-2) - 6 = -14 \rightarrow k$ | $y = -(3)^2 + 6(3) + 3 = 12 \rightarrow k$ |
| $f(x) = a(x-h)^2 + k$ | $f(x) = a(x-h)^2 + k$ |
| $f(x) = 2(x2)^2 - 14$ | $f(x) = -1(x-3)^2 + 12$ |
| $f(x) = 2(x+2)^2 - 14$ | or $f(x) = -(x-3)^2 + 12$ |

Part Seven: Applications of Quadratic Functions

Solve the following word problems.

26) A person standing at the edge of a building throws a baseball vertically upward. The quadratic function $f(x) = -16x^2 + 64x + 32$ models the baseball's height above the ground, f(x) in meters, x seconds after it was thrown.

a) From what height was the baseball thrown?

starting value \rightarrow y-intercept (plug in 0 for x)

 $f(0) = -16(0)^2 + 64(0) + 32 = 32$ meters

b) When did the baseball hit it's maximum height?

x-value of vertex

 $x = \frac{-b}{2a} = \frac{-64}{2(-16)} = \frac{-64}{-32} = 2$ seconds

c) What was the baseball's maximum height?

y-value of the vertex \rightarrow plus in the x-value of the vertex (2) to find the y-value

 $f(2) = -16(2)^2 + 64(2) + 32 = 96$ meters

d) A bird is flying 100 feet above the ground - is the bird in danger of being hit?

No - the baseball reaches a maximum height of only 96 meters so it will not hit the bird

e) When did the baseball land?

Jennifer hit a golf ball from the ground and it followed the projectile $h(t) = -16t^2 + 100t$, where t is the time in seconds, and h is the height of the ball.

a) When did the ball hit it's maximum height?

x-value of vertex

 $x = \frac{-b}{2a} = \frac{-100}{2(-16)} = \frac{-100}{-32} = 3.125 \text{ seconds}$

b) What was the maximum height?

y-value of the vertex \rightarrow plus in the x-value of the vertex (3.125) to find the y-value

 $f(2) = -16(3.125)^2 + 100(3.125) =$ **156**. **25** *meters*

c) When did the golfball land?